

Modeling and Simulation of Hybrid Energy System Supplying 3 \emptyset Load and its Power Quality Analysis

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Abstract- The proposed Hybrid Energy System (HES) consists of solar photovoltaic (PV) system, the electrolyzer, the storage tank and the solid oxide fuel cell (SOFC). The HES is used to supply the electricity to the 3 \emptyset load as well as 1 \emptyset load which is synchronized to the grid with the help of voltage source converter (VSC). In this technology when PV power is not sufficient to fulfill the load demand, then SOFC power is utilized to fulfill the required demand. A fuel cell controller is proposed in which a PID controller is used to regulate the amount of hydrogen (H₂) flow through the valve and utilized as a fuel of SOFC. In this paper, H₂ is generated from electrolyzer which takes extra PV energy and water as input elements. The complete modeling of the individual components is simulated in Matlab/Simulink environment and also the results obtained are found to be satisfactory. Then power quality factor is verified for HES as well as 3 \emptyset non-linear load to analyze the quality of power.

Keywords- Harmonic distortion, power quality, PV cell, SOFC, electrolyzer, grid

1. Introduction

The renewable energy sources (RESs) are clean energy sources and more reliable in nature. Photo voltaic energy sources, tidal energy sources, wind energy sources and micro-turbines, etc. are the numerous RESs employed in the hybrid energy system [1-2]. In the current research area, the generation of electric energy is proposed for the rural consumers where there is no grid connection. For such areas RESs is the better solution for generation of decentralized power. For such power generation the combination of hydro, wind and PV are the environmental friendly and cost effective according to [3, 27-28, 33-34]. Innovation of the technology is needed to utilize these RESs for the power generation and to obtain the better efficiency. A HES consisting of combination of PV-wind-diesel is used in [4]. But due to increasing cost of diesel and use of the diesel environmental pollution is created that makes the operation of diesel engine prohibited. A HES consisting of a wind-hydro is connected to the grid where the power converters are used to improve the reliability of the power system [5]. The cost and reliability of the HES for the

distant and remote places evaluated by the optimization technique are shown in [6]. Now-a-day's many works have been carried out for the analysis of power quality study of the RES consisting of PV, wind and other renewable sources.

A maximum power point tracking (MPPT) is used in PV system to extract maximum power according to procedure adopted in [7]. In recent years, wind energy system (WES) becomes most important energy generating source. However, WES depended on the natural wind speed. Also maximum power point tracker is used to extract maximum power as shown in [8-9]. The grid integration of renewable energy sources along with its challenges, issues and possible solutions has been described by Anees, *et al* [10]. An efficient voltage regulation scheme for three-phase self-excited induction generator feeding single-phase load in remote locations has been identified by Gao, *et al* [11]. Hasaneen, *et al* [12] have discussed the design and simulation of DC/DC boost converter. A comparison of two MPPT techniques for PV system in Matlab/Simulink has been made by Kondawar, *et al* [13]. [14 & 29] give the information about the interconnecting issues of photovoltaic/wind hybrid system with electric utility using

artificial intelligence. An improved power conditioning system for grid integration of photovoltaic solar energy conversion systems has been studied by Molina, *et al* [15]. Murthy, *et al* [16] have developed a microhydel grid independent power generation scheme using induction generators for Indian conditions. A wind energy conversion scheme using a self-excited induction generator has been proposed by Raina, *et al* [17]. Fault analysis of grid connected photovoltaic system has been studied by Hota, *et al* [18]. A novel hybrid integrated wind-PV micro co-generation energy scheme for village electricity has been discussed by Sharaf, *et al* [19]. Doron [20] has presented the definition of total harmonic distortion and its effect on measurement interpretation. Then the Power Quality Factor (PQF) describes the power transfer quality of the 3Ø supply connected to the load [21].

In this paper, modeling and simulation is done for a novel HES consisting of PV, electrolyzer, SOFC and storage Tank. Then this HES is connected to the grid by means of VSC in order to achieve continuous power supply to the load. A fuel cell controller is considered for the HES consisting of a PID controller and a valve, where the PID controller is used to control the valve because the flow of hydrogen to the SOFC is regulated through the valve according to the load requirement. The advantages HES connected to the grid make the uninterrupted power supply to the load. From the literature survey it appears that not much research has been done on power quality analysis of HES consisting of PV, electrolyzer and fuel cell. To analyze the power quality a single indicator known as power quality factor (PQF) is considered. It can be mentioned that the quality of low power transfer is caused due to the supply voltage (voltage harmonics or unbalanced voltage supply) or due to the load (unbalanced or nonlinear load) or due to both of them. So, PQF gives quick assessment of the quality of the transfer power at any selected point of the supply. Hence, the power quality analysis is considered to calculate the quality of power transfer of the HES supplying 3Ø non-linear load.

2. Description of Grid Connected Hybrid Energy System

The proposed HES model is given in Fig.1. In this model, it is shown that the PV with maximum power point tracker (MPPT) tracks the maximum output power which is given to the DC/DC converter (boost converter) to increase the DC voltage. Then this voltage is given as the input of DC/AC converter, which converts DC voltage to AC voltage and this AC voltage is used to fulfill the load requirement. The extra power if any is given to the electrolyzer which converts water into H₂ and oxygen. Hence, H₂ is used as a fuel of SOFC and the amount of flow of H₂ to SOFC is regulated by the PID controller through the valve. When the PV power is not sufficient to fulfill the load demand then SOFC fulfills the required demand. Also, the HES is connected to the grid through VSC. In this chapter PQF analysis is done to measure the quality of power which is supplied to the 3Ø non-linear load from HES.

2.1 Modeling of Photovoltaic (PV) System

Basically, a PV cell is a p-n junction semiconductor diode where the sun energy falls on the PV cell surface, then it produces the DC power. By using the eq. (1) the PV model is designed. Fig.2 shows the single diode model of PV array and Table 1 contains specifications of the photovoltaic (PV) array. Sun power SRP- 305-WHT solar panel is chosen for modeling and simulation by the help of Matlab according to [18, 25, 26, 30-32].

$$V_{pv} = \frac{N_s a k T}{q} \ln \left[\frac{I_{sc} - I_{pv} + N_p}{N_p I_0} \right] - \frac{N_s}{N_p} R_s I_{pv} \quad (1)$$

Parameters used to design the PV model:

- I₀ : Reverse saturation current of PV cell, [A]
- I_{sc} : short-circuit PV cell current, [A]
- I_{pv}/I_{ph} : Output current of PV cell, [A]
- k : Boltzmann's constant, [J/°K]
- a : completion or ideality factor
- q : electron charge, [C]
- R_p : PV cell containing parallel resistance, [Ω]
- R_s : PV cell containing series resistance, [Ω]
- N_s : No. of series cells in a string of the PV cell
- N_p : No. of parallel strings
- T : Temperature of the PV cell, [K]
- V_{PV} : PV cell terminal voltage in volt, [V]
- V_{MP} : The voltage related to maximum power of the PV cell, [V]
- V_{OC} : PV cell open-circuit voltage in volt, [V]

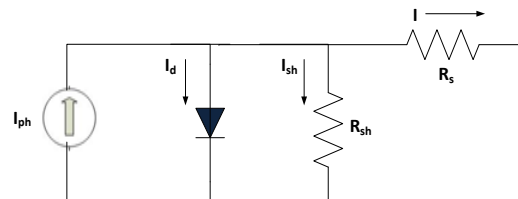


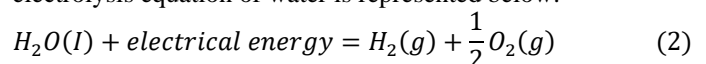
Fig. 2. Single diode model of the PV Array

Table 1 Specifications of photovoltaic (PV) array

Specification	Value
No. of series connected PV cell	96
No. of Modules in parallel	66
No. of Modules in series	05
Open circuit voltage(V _{OC})	64.2 V
Short circuit current(I _{SC})	5.96 A
Maximum Power of PV cell	305W
Temperature(T)	25
Irradiance	1000

2.2 Modeling of Electrolyzer

The water is decomposed into hydrogen (H₂) and oxygen through the electrolyzer by using the extra power of PV. The electrolysis equation of water is represented below:



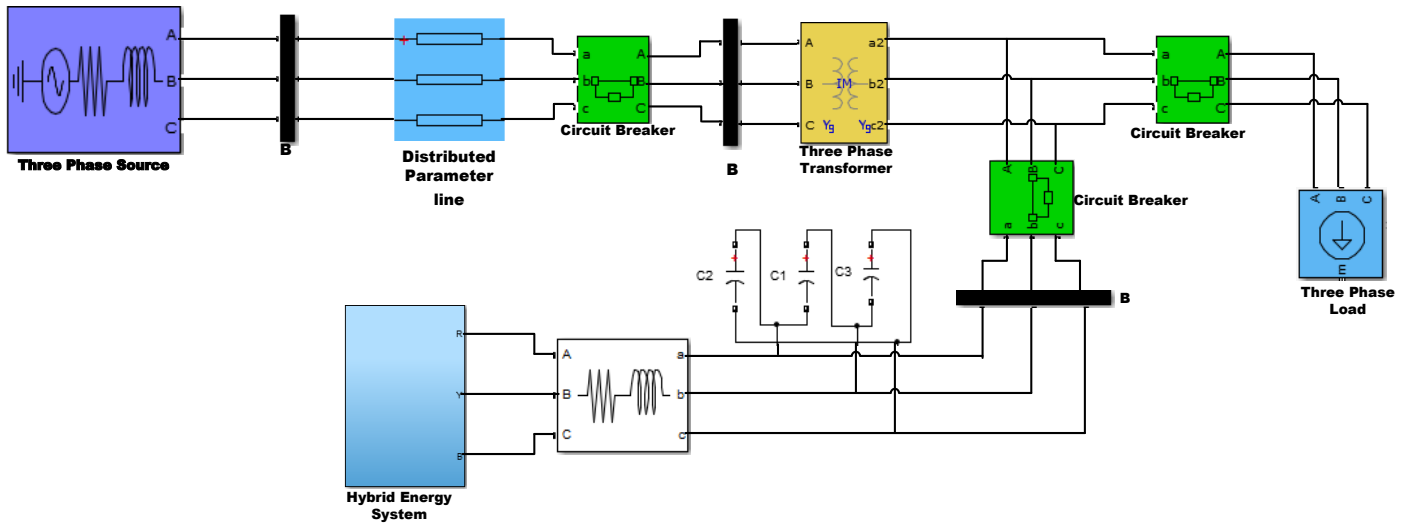


Fig. 1. The proposed model of hybrid energy system connected to grid

Parameters of an electrolyzer model are given below:

- i_e : Current of an electrolyzer, [A]
- n_c : No. of series connected electrolyzer cells
- nH_2 : Amount of hydrogen generated in moles per second, [mol s⁻¹]
- F : Faraday constant, [C kmol⁻¹]
- η_F : Faraday efficiency

According to Faraday's law, there is direct relation between hydrogen production through the electrolyzer and electrical current given below [25].

$$nH_2 = \frac{n_F n_c i_e}{2F} \quad (3)$$

Faraday efficiency is given in terms of hydrogen generation and its theoretical value which is shown below.

$$\eta_F = 96.5e \left(\frac{0.09 - 75.5}{i_e - i_e^2} \right) \quad (4)$$

Fig. 3 shows the model of electrolyzer by using the eqs. (3) and (4).

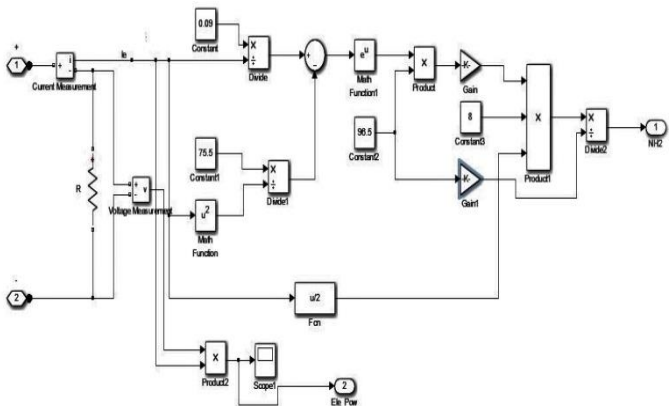


Fig. 3. A brief model of electrolyzer using Simulink

2.3 Modeling of Storage Tank

Storage tank is used to store the H₂, which is generated

from the electrolyzer. Further this H₂ is used as a fuel of SOFC. Eq. (5) shows the design model of storage tank.

$$P_b - P_{bi} = z \frac{NH_2 RT_b}{MH_2 V_b} \quad (5)$$

Parameters of the storage tank are given below:

- Z : Pressure compressibility factor
- NH_2 : Amount of hydrogen stored in the storage tank in moles per second, [kmol s⁻¹]
- MH_2 : Hydrogen molar mass, [kg kmol⁻¹]
- T_b : operating temperature, [°K]
- P_{bi} : Storage tank pressure at initial stage, [Pa]
- P_b : Storage tank pressure, [Pa]
- R : Rydberg/Universal gas constant, [J (kmol °K)⁻¹]
- V_b : Storage tank volume, [m³]

A model of hydrogen storage tank is shown in Fig.4.

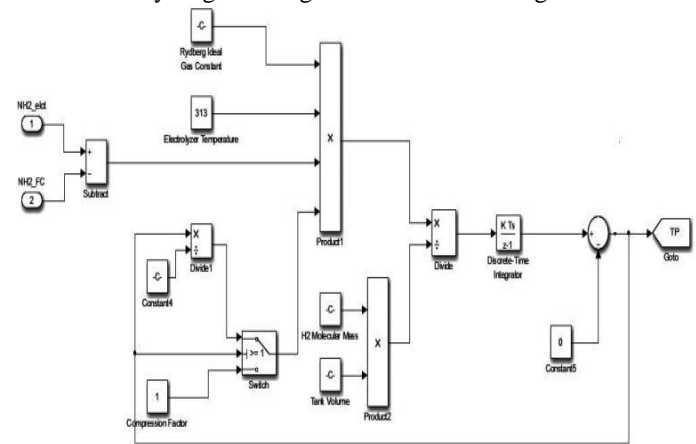


Fig. 4. A brief model of hydrogen storage tank using Simulink

2.4 Modeling of SOFC

SOFC parameters are shown below that has been used to design the model of SOFC [23].

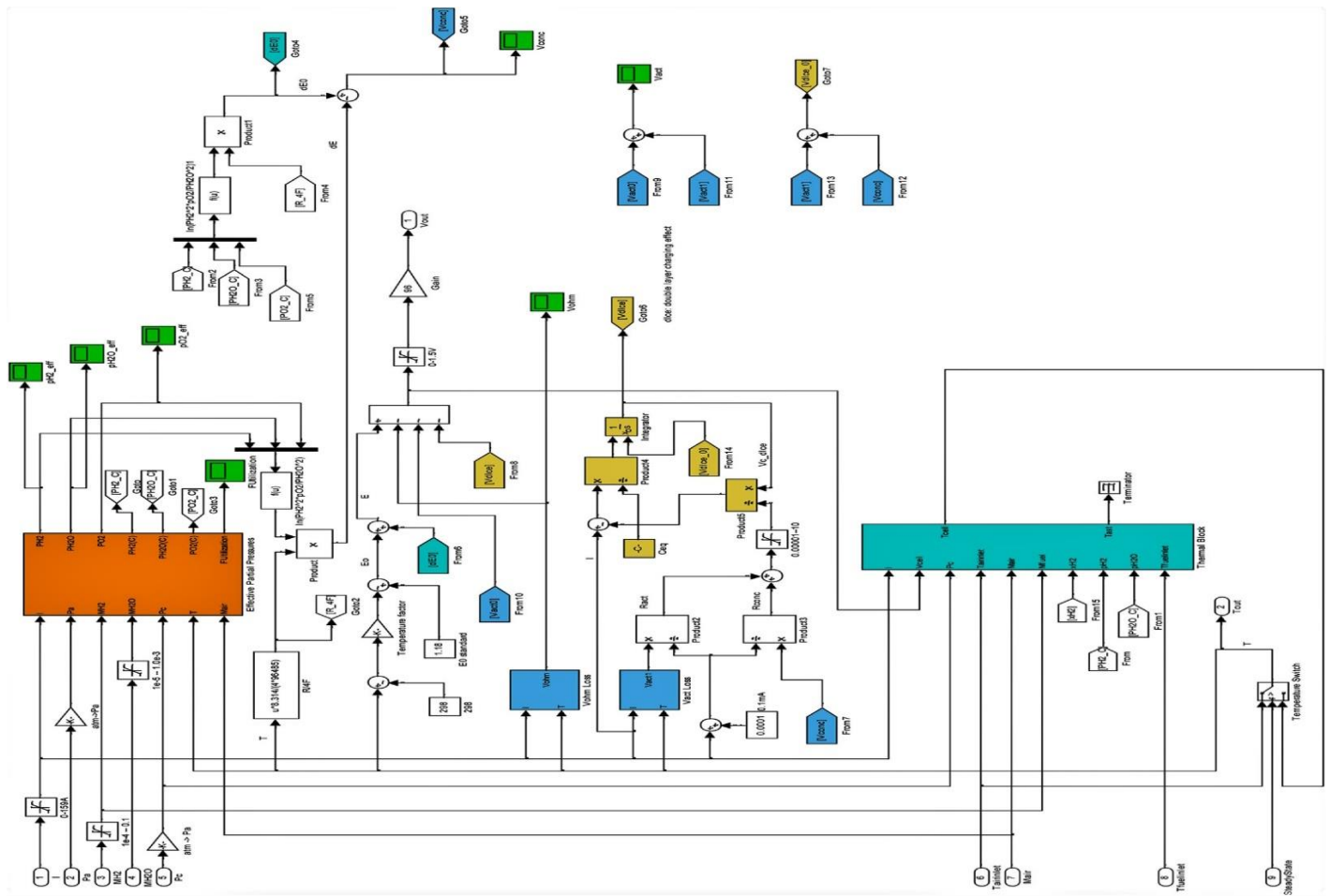


Fig. 5. A brief model of SOFC system using Simulink

B and C : Activation voltage constants are used to simulate SOFC system, [V]

CV : conversion factor, $\left[\frac{\text{Hydrogen(kmol)}}{\text{Methane(Kmol)}} \right]$

E_0 : normal no load voltage, [V]

E : Nernst immediate voltage, [V]

F : Faraday's constant, [C (kmol⁻¹)]

I_{FC} : feedback current of SOFC, [A]

k_1 : gain of PI (proportional-integral)

K_{an} : anode valve constant, $\left[\sqrt{\text{kmol kg(atm s)}^{-1}} \right]$

K_r : modeling constant, [kmol SA⁻¹]

K_{H_2O} : molar constant of water valve, [kmol (atms⁻¹)]

K_{H_2} : molar constant of hydrogen valve, [kmol (atm s⁻¹)]

K_{O_2} : molar constant of oxygen valve, [kmol (atm s⁻¹)]

M_{H_2} : hydrogen molar mass, [kg kmol⁻¹]

P_{H_2O} : water fractional pressure, [atm]

P_{H_2} : hydrogen fractional pressure, [atm]

P_{O_2} : oxygen fractional pressure, [atm]

N_0 : No. of fuel cells are in series in a stack

q_{H_2} : molar flow of hydrogen, [kmols⁻¹]

$q_{methane}$: methane flow rate, [kmols⁻¹]

q_{O_2} : input molar flow of oxygen, [kmols⁻¹]

$q_{H_2}^{in}$: input flow of hydrogen, [kmols⁻¹]

$q_{H_2}^{out}$: hydrogen output flow, [kmols⁻¹]

$q_{H_2}^r$: hydrogen flow amount that reacts, [kmols⁻¹]

$q_{H_2}^{req}$: hydrogen flow amount that meets load change, [kmols⁻¹]

R : Rydberg (Universal) gas constant, [(1atm) (kmol K)⁻¹]

R_{int} : internal resistance of SOFC, [Ω]

T : absolute temperature, [K]

U : utilization rate τ

V_{an} : volume of the anode, [m³]

V_{cell} : SOFC dc output voltage, [V]

τ_1, τ_2 : reformer time constants, [s]

τ_3 : PI controller time constant, [s]

τ_{H_2} : hydrogen time constant, [s]

τ_{H_2O} : water time constant, [s]

τ_{O_2} : oxygen time constant, [s]

Z_{act} : activation over voltage, [V]

Z_{ohmic} : ohmic over voltage, [V]

The ratio of the molar flow of hydrogen and hydrogen partial pressure in a channel is given in [23].

$$\frac{q_{H_2}}{P_{H_2}} = \frac{K_{an}}{\sqrt{M_{H_2}}} = K_{H_2} \quad (6)$$

Three factors are considered for the hydrogen flow namely hydrogen input and output flow and hydrogen flow at the time of reaction [22]. So, the required equation is developed as:

$$\frac{d}{dt} p_{H_2} = \frac{RT}{V_{an}} (q_{H_2}^{in} - q_{H_2}^{out} - q_{H_2}^r) \quad (7)$$

The flow of reacted hydrogen is shown below [22].

$$q_{H_2}^r = \frac{N_0 I_{FC}}{2F} = 2K_r I_{FC} \quad (8)$$

The partial pressure of hydrogen is shown below by using Laplace transform of the eqs. (6) and (8).

$$P_{H_2} = \frac{1/K_{H_2}}{1 + \tau_{H_2} s} (q_{H_2}^{in} - 2K_r I_{FC}) \quad (9)$$

where, τ_{H_2}

$$= \frac{V_{an}}{K_{H_2} RT} \quad (10)$$

The output voltage of SOFC can be determined by considering the activation over voltage, Nernst's voltage and the ohmic over voltage as given in [22].

$$V_{cell} = E + \eta_{act} + \eta_{ohmic} \quad (11)$$

Where,

$$\eta_{act} = -B \ln(CI_{FC}) \quad (12)$$

And

$$\eta_{ohmic} = -R^{int} I_{FC} \quad (13)$$

So, Nernst voltage is obtained which is given in [22].

$$E = N_0 \left[E_0 + \frac{RT}{2F} \log \left[\frac{P_{H_2} \sqrt{P_{O_2}}}{P_{H_2O}} \right] \right] \quad (14)$$

The SOFC takes H₂ as a fuel for the required power demand. The continuous supply of hydrogen is possible with the help of the reformer. The modeling of the reformer is given in eq. (15).

$$\frac{q_{H_2}}{q_{methanol}} = \frac{CV}{\tau_1 \tau_2 s^2 + (\tau_1 + \tau_2)s + 1} \quad (15)$$

SOFC output current is used as the input of the SOFC to determine the required amount of hydrogen that flow to the SOFC.

$$q_{H_2}^{req} = \frac{N_0 I_{FC}}{2FU} \quad (16)$$

The available hydrogen of the reformer further utilized to maintain flow of methane by using the PI controller. It can be expressed as:

$$q_{methane} = \left(k_1 + \frac{k_1}{\tau_3 s} \right) \left(\frac{N_0 I_{FC}}{2FU} - q_{H_2}^{in} \right) \quad (17)$$

Table 2 Specifications of SOFC to design the mathematical mode

Specification	Value
Activation voltage constant (B)	0.04777 [A ⁻¹]
Activation voltage constant (C)	0.0136 [V]
Conversion factor (CV)	2
Faraday's constant (F)	96 484 600 [Ckmol ⁻¹]
FC system internal resistance (R _{int})	0.26664 [Ω]
FC absolute temperature (T)	343 [K]

Hydrogen time constant (τ _{H2})	3.37 [s]
Hydrogen valve constant (K _{H2})	4.22 x 10 ⁻⁵ [kmol (s atm) ⁻¹]
Hydrogen-oxygen flow ratio (r _{H2O})	1.168
Kr constant = N ₀ /4F	2.2802 x 10 ⁻⁷ [kmol (s A) ⁻¹]
Line reactance (X)	0:0809 [Ω]
Methane reference signal (Q _{methref})	0.000015 [kmol s ⁻¹]
No load voltage (E _o)	1.18 [V]
Number of cells (N _o)	88
Number of stacks (N _s)	1
Oxygen time constant (τ _{O2})	6.74 [s]
Oxygen valve constant, (k _{O2})	2.11 x 10 ⁻⁵ [kmol (s atm) ⁻¹]
PI gain constant (k _i)	0.25
Reformer time constant (τ ₁ , τ ₂ , τ ₃)	15 [s]
Universal gas constant (R)	8314.47 [J kmolK ⁻¹]
Utilization factor (U)	0.8
Water time constant (τ _{H2O})	18.418 [s]
Water valve constant (K _{H2O})	7.716 x 10 ⁻⁶ [kmol (s atm) ⁻¹]

A SOFC with the range of 5 KW is developed by the help of the above parameters as given in Table 2 and a SOFC model is shown in Fig.5 as given in [24]. For this proposed model three 5 KW SOFC are used.

2.5 Internal Structure of Proposed Hybrid Energy System

Fig.6 shows the internal structure of the proposed hybrid energy system (HES) which is represented in Fig.1. PV system with MPPT tracks the maximum power, which is further utilized to fulfill the required demand of the load. The electrolyzer connected across the buck converter used the extra amount of PV power to extract the H₂ from water according [6]. Hence, this H₂ is used for the fuel of SOFC. A DC-DC converter is connected to PV with MPPT to increase the voltage; also this converter is triggered by the MPPT generated gate pulse. Again another DC/DC converter is used to increase the voltage level of SOFC as shown in Figs.6 and 7. From the Fig.6, it can be seen that the HES is connected to grid with the help of voltage source converter (VSC) to synchronize the HES voltage with the grid voltage. VSC contains two controlled cascade loops that are described below.

Voltage controller of DC-link: Active power and its desired value is controlled by the DC-link voltage controller. i_d* of the DC-link PI controller is used as a reference which is compared with the i_d shown in Fig.8.

Internal current loop: The grid voltage (V_a, V_b, V_c) and grid current (i_a, i_b, i_c) are transformed to d-q reference frame with the help of abc/dq controller or synchronous reference frame (SRF). DC values are determined by using the SRF because these values are easier to control and design. Hence, these are used for controlling the variables. Phase angle is derived by the PLL (phase locked loop), where grid voltage acts as the input of PLL.

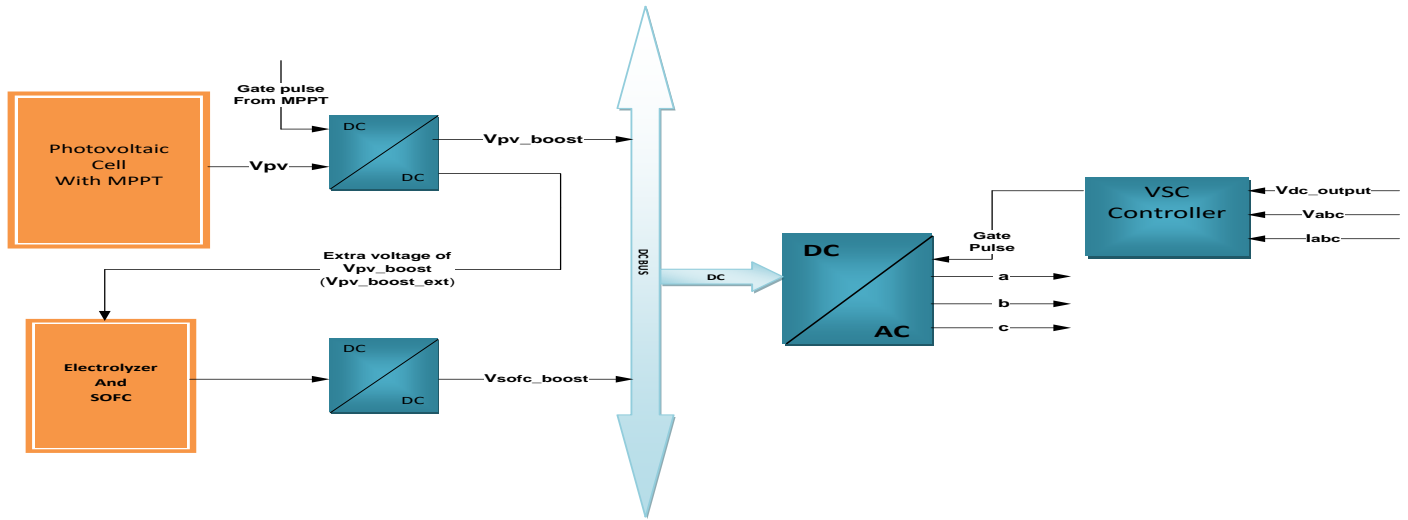


Fig. 6. Block diagram of hybrid energy system (HES)

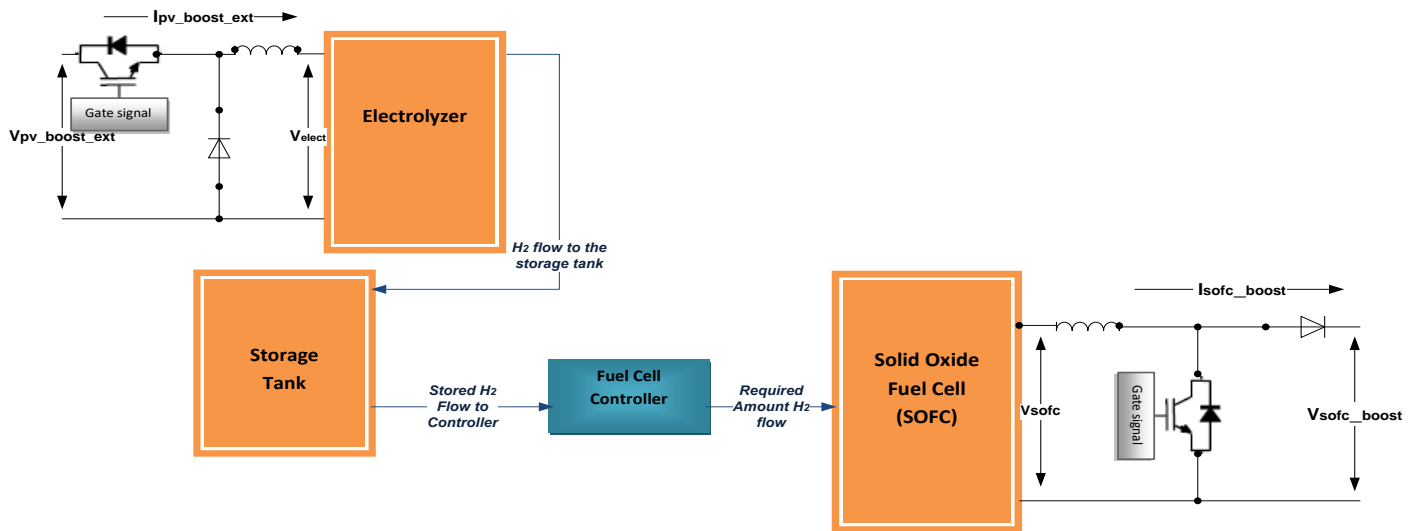


Fig. 7. Block diagram representation of hydrogen flow from electrolyzer to SOFC

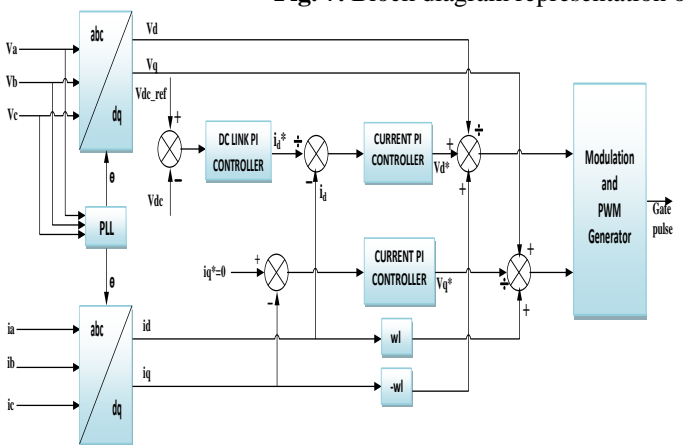


Fig. 8. Block diagram representation of voltage source inverter (VSC)

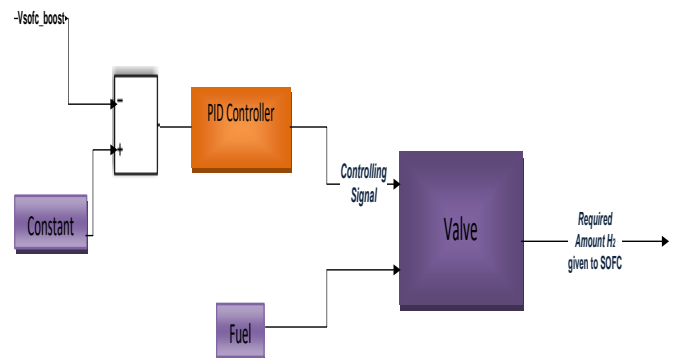


Fig. 9. Block diagram representation of fuel cell controller

As shown in Fig.8, the reference frame voltages (V_d, V_q) are synchronized with the controlled currents. Further i_q^* (reference

reactive current) is set to zero value as shown in Fig.8. Hence, power factor is to maintain as unity. The voltages (V_d^* , V_q^*) of the current PI controllers are used as the input of the PWM generator, which produces pulses to trigger the DC/AC converter [24].

Fig.7 shows that an electrolyzer is connected to buck converter, which takes the PV power and that power further utilized by the electrolyzer to convert the water into H₂ and oxygen. Then this H₂ is used as fuel of SOFC to fulfill the load requirement when the PV power is not sufficient for the required load and the rest amount of hydrogen is stored in storage tank for future requirement. Fig.9 represents fuel cell controller block diagram. In this block *Vsofc_boost* (voltage of boost converter connected to SOFC) is compared with the constant value and given to the PID controller. The output signal of the PID controller controls the valve, where the amount of H₂ flows according to the load demand. The PID controller values are set by the help of self tuned mode provided in the PID controller block (P=0.00013317, I = 3.3925227e-05, D = -6.254254172870e-05).

3. Operational Control Strategy of Hybrid Energy System

Operational control strategy is used to manage the correlation between the HES and load demand. It attends the 4 possible ways to supervise the proposed system.

(i) If Load power (Pload) < PV power (Ppv), at that time PV power carry out the load demand and the extra amount of PV power is utilized by the electrolyzer, which converts water into H₂ and oxygen and later this H₂ is used as a fuel of SOFC.

(ii) If Load power (Pload) > PV power (Ppv), at that time PV is not enough to fulfill the required load. So, SOFC is used to fulfill the required demand with PV.

(iii) If Load demand (Pload) = PV power (Ppv), at that time PV power satisfy the required load. So, no extra power is supplied to electrolyzer.

(iv) If PV power (Ppv) is zero, at that time PV does not supply any power. So, required load demand is fulfilled by the SOFC.

In this manner the operational control strategy operates. In case the PV as well as SOFC fails to supply the power, then the grid continuously supplies to the load and provides the uninterrupted power supply to the load.

4. Analysis of Power Quality Factor (PQF)

The power quality factor (PQF), a single indicator ranging from 0 to 1 is used to measure the quality of power transfer of a HES connected to grid supplying the 3Ø load. The aspects considered for power quality are: harmonic levels of the voltage and current; unbalanced 3Ø voltage and current; and phase displacement factor of different phases on the basis of their fundamental frequency. The PQF is unity when a balanced sinusoidal voltage and current is supplied by the network at the zero phase displacement. PQF depends on the following three aspects described below.

A. Harmonics levels of the voltage and current

VTHD and ITHD are the voltage and current total harmonic distortions respectively for a 3Ø or a 1Ø circuits.

$$[VTHD]^2 = \frac{\sum_{h \neq 1} V_h^2}{V_1^2} \quad (18)$$

$$[ITHD]^2 = \frac{\sum_{h \neq 1} I_h^2}{I_1^2} \quad (19)$$

where, V and I represent rms values; h and 1 represents the harmonic order and fundamental, respectively.

Lower order harmonics cause lesser losses than the higher order harmonics with the same amplitude. So, the voltage and current total adjusted harmonics distortion are given below.

$$[VTHD]_{H-A}^2 = \frac{\sum_{k \neq 1} (C_h V_h)^2}{V_1^2} \quad (20)$$

$$[ITHD]_{H-A}^2 = \frac{\sum_{k \neq 1} (D_h I_h)^2}{I_1^2} \quad (21)$$

where, $C_h, D_h =$ weighting factors (> 1).

Eqs.(18) and (19) can be extended to a 3Ø network as given in [21].

$$V_{eH}^2 = \sum_{h \neq 1} \frac{V_{ah}^2 + V_{bh}^2 + V_{ch}^2}{3} \quad (22)$$

$$I_{eH}^2 = \sum_{h \neq 1} \frac{I_{ah}^2 + I_{bh}^2 + I_{ch}^2}{3} \quad (23)$$

$V_{eH}, I_{eH} =$ equivalent harmonics rms voltage and current of the 3Ø network. The eqs. (22) and (23) are used in (20) and (21). Hence, the equivalent adjusted harmonics values are formed that is given below.

$$V_{eH-A}^2 = \sum_{h \neq 1} C_h^2 \frac{V_{ah}^2 + V_{bh}^2 + V_{ch}^2}{3} \quad (24)$$

$$I_{eH-A}^2 = \sum_{h \neq 1} D_h^2 \frac{I_{ah}^2 + I_{bh}^2 + I_{ch}^2}{3} \quad (25)$$

So, QA_1 and QA_2 are the quality aspects of total harmonics destruction of voltage and current (VTHD and ITHD) of the 3Ø network.

$$QA_1 = VTHD = \frac{V_{eH-A}}{V_{e1}} \quad (26)$$

$$QA_2 = ITHD = \frac{I_{eH-A}}{I_{e1}} \quad (27)$$

where, $V_{e1}, I_{e1} =$ equivalent fundamental phase voltage and current of the 3Ø network.

$$V_{e1}^2 = \frac{V_{a1}^2 + V_{b1}^2 + V_{c1}^2}{3} \quad (28)$$

$$I_{e1}^2 = \frac{I_{a1}^2 + I_{b1}^2 + I_{c1}^2}{3} \quad (29)$$

Eqs. (22) to (25), (28) and (29) show about the losses of the 3Ø network. So, some assumptions are shown below:

(1) At a particular frequency the losses of line as well as equipment are related to square of the particular voltage and current.

(2) Parameters of line as well as equipment are symmetrical.

B. Unbalanced 3Ø voltage and current

In a 3Ø networks the power transfer quality is affected due to the unbalanced current and voltage; also many aspects are responsible for this, these are line losses occurs at the same power level, additional losses are occurred in the overloading

neutral conductors as well as in drives in a 4-wire distribution system. So, a 3ϕ sinusoidal voltage network $[V_a, V_b, V_c]$ is decomposed into following three parts.

$$\left. \begin{aligned} \underline{V}^+ &= \frac{1}{\sqrt{3}}(\underline{V}_a + a\underline{V}_b + a^2\underline{V}_c) \\ \underline{V}^- &= \frac{1}{\sqrt{3}}(\underline{V}_a + a^2\underline{V}_b + a\underline{V}_c) \\ \underline{V}^0 &= \frac{1}{\sqrt{3}}(\underline{V}_a + \underline{V}_b + \underline{V}_c) \end{aligned} \right\} \quad (30)$$

where, \underline{V} = phasor of V and $a = \exp(j2\pi/3)$. So from eqs. (28) to (30) equivalent voltage is found out.

$$V_{e1}^2 = \underline{V}^{+2} + \underline{V}^{-2} + \underline{V}^{02} \quad (31)$$

Also the current equations can be written in same manner as voltage is written in eqs (30) and (31). Hence, the quality aspects $[QA_3$ and $QA_4]$ can be identified as unbalanced voltage and current factors.

$$QA_3 = \frac{[V_{e1}^2 - (V^+)^2]^{\frac{1}{2}}}{V_{e1}} \quad (32)$$

$$QA_4 = \frac{[I_{e1}^2 - (I^+)^2]^{\frac{1}{2}}}{I_{e1}} \quad (34)$$

C. Phase displacement factor of different phases on the basis of their fundamental frequency.

In the power transfer situation phase displacement among the voltage and current at fundamental frequency gives the information about the utilization of the equipment of the generation as well as distribution. Traditionally in the 1ϕ situation the power factor (pf) can be expressed as the ratio of the active power (P) and the apparent power (S), also the power is the rms voltage and current.

But, in non-sinusoidal case power factor above described to be confusing. So, according to [21] instantaneous power is the product of voltage and current instantaneous values. Hence, the active power (P) is derived from the averaging of instantaneous power with respected to time. But, there is no physical meaning of the apparent power (S), hence the voltage and current values are not considered at each instant. When instantaneous voltage and current uphold a constant ratio; at that time apparent power (S) equals to P .

All the incompleteness and ambiguities written above can be avoided when a physical entity is directly responsible for utilization of the poor power capacity at the considered fundamental frequency. Hence, the phase difference occurs in the voltage and current having the fundamental frequencies at the load side or source side. So, this aspect is reflected in the power quality and hence, a new factor is considered known as orthogonal current factor (OCF) according to [21].

$$OCF = \frac{I_{1a}\sin\theta_{1a} + I_{1b}\sin\theta_{1b} + I_{1c}\sin\theta_{1c}}{I_{1a} + I_{1b} + I_{1c}} \quad (34)$$

$$QA_5 = |OCF| \quad (35)$$

where, I_{1a} , I_{1b} and I_{1c} = rms values of phase currents at the fundamental frequency. θ_{1a} , θ_{1b} and θ_{1c} = phase differences between voltages and currents at fundamental frequency components.

PQF (a single measurable indicator) is used to reflect different various power quality aspects according to [21] that can be expressed as:

$$PQF = \sum_i w_i(1 - QA_i) \quad (36)$$

where, w_i = weighting factor ($\cong 1$). It is different for the different consumers and recommendation of the weighting factor is supported by the economics studies according to [21]. It can be chosen to show economical and technical priorities in different environments.

QA_i = different quality aspects

The PQF is unit or ideal when the loaded network is balanced having sinusoidal voltages and currents with phase displacement is zero. PQF value is low due to the poor uses of the power capacity of the source or due to the harmonics containing higher level or due to unbalance between different phases.

5. Simulation Results and Discussion

The proposed HES described above has been designed in MATLAB/Simulink environment and also the performance characteristics of this system are verified on different conditions. Hydrogen (H_2) generation from the electrolyzer is

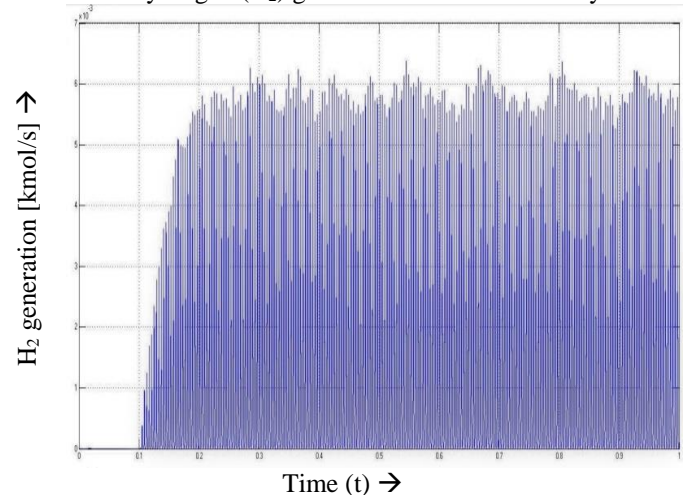
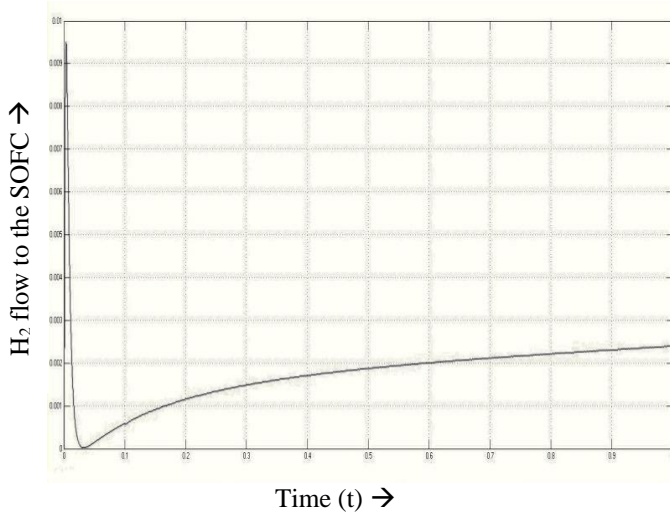


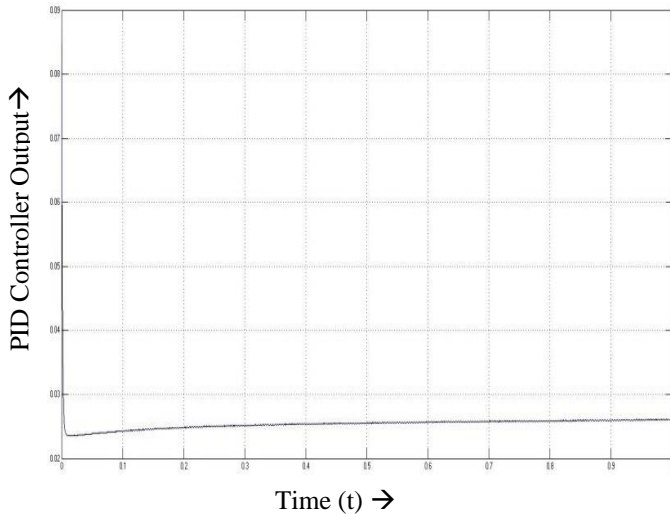
Fig. 10. H_2 generation by Electrolyzer

achieved by taking the extra amount of PV power shown in Fig.10 and this hydrogen is used as fuel of the fuel cell (SOFC) because this hydrogen is used to flow to SOFC through the valve which is shown in Fig.11a to fulfill the required demand when the PV power is not sufficient to fulfill the requirement load. Hence, the hydrogen flow through the valve is controlled by the PID controller. Accordingly, Fig.11b shows the output of the PID controller.

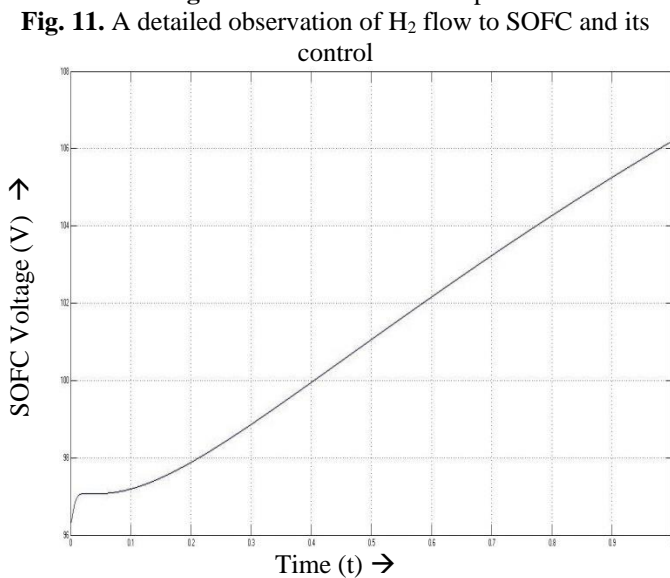
Output voltage of a 5KW SOFC is shown in Fig.12a. Three nos. of 5KW SOFC are connected in series, whose output voltage is shown in Fig.12b.



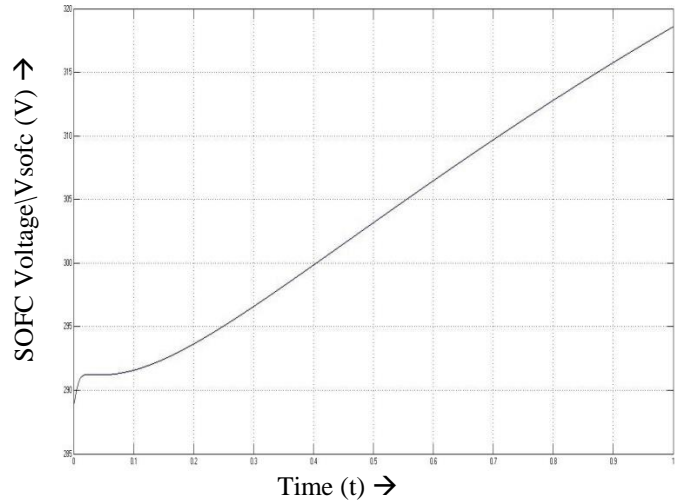
Time (t) →
Fig. 11a. H₂ flow to the SOFC



Time (t) →
Fig. 11b. PID Controller Output



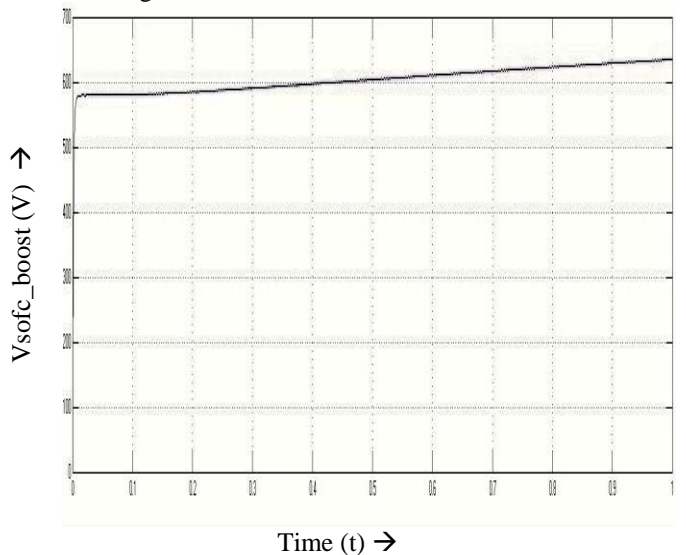
Time (t) →
Fig.12a. Output voltage of a 5 KW SOFC



Time (t) →
Fig.12b. Output voltage of 3 nos. of 5KW SOFC
Fig.12. Output voltage of the SOFC

Output voltage of a 5KW SOFC is shown in Fig.12a. Three nos. of 5KW SOFC are connected in series, whose output voltage is shown in Fig.12b.

This output voltage of SOFC is increased by the help of boost converter (DC/DC converter) as shown in Fig.13 and used for fulfilling the demanded load; when PV power is not sufficient. Fig.14 shows the waveforms for the voltage and current of HES supplied to the 3Ø non-linear load. Similarly, Fig.15 shows the waveforms for voltage, current and power of a 3Ø non-linear load with the active power (P) = 8000W, inductive power (Q_L) = 2000VAR and capacitive power (Q_C) = 100VAR. Hence, this HES is used to fulfill the 3Ø load demand. Also, HES is used for domestic purposes and gives the clean energy sources. Further, HES is cheaper when it is used for a domestic purpose in a colony based system, when more than 3 consumers are supplied by the HES system connected to grid.



Time (t) →
Fig. 13. Output voltage of boost converter connected to SOFC

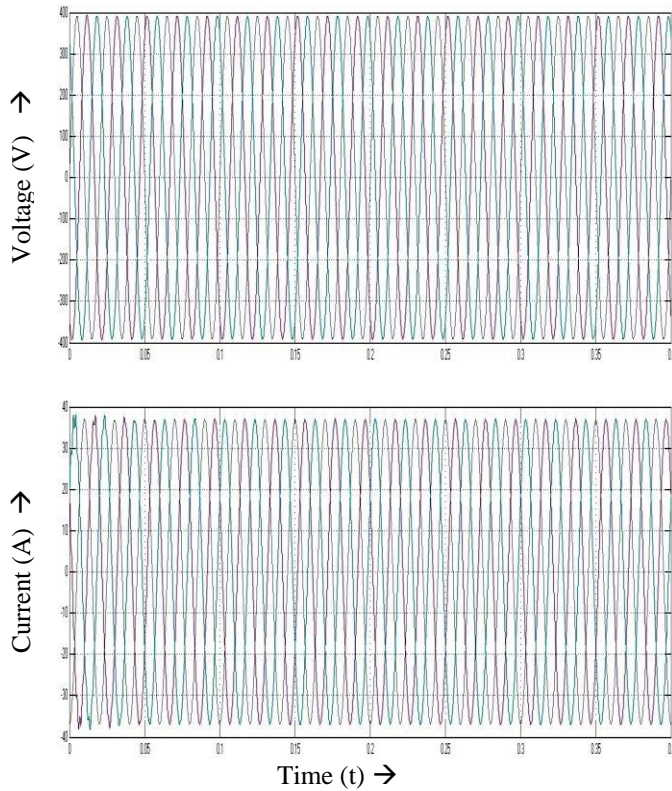


Fig. 14. Output voltage and current of hybrid energy system (HES)

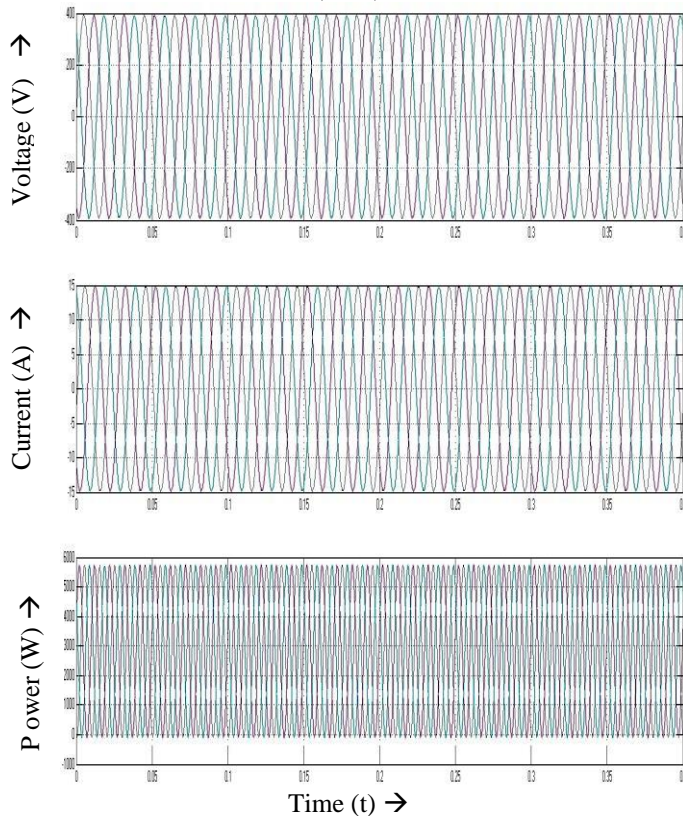


Fig. 15. Voltage, current and power of a 3 ϕ non-linear load

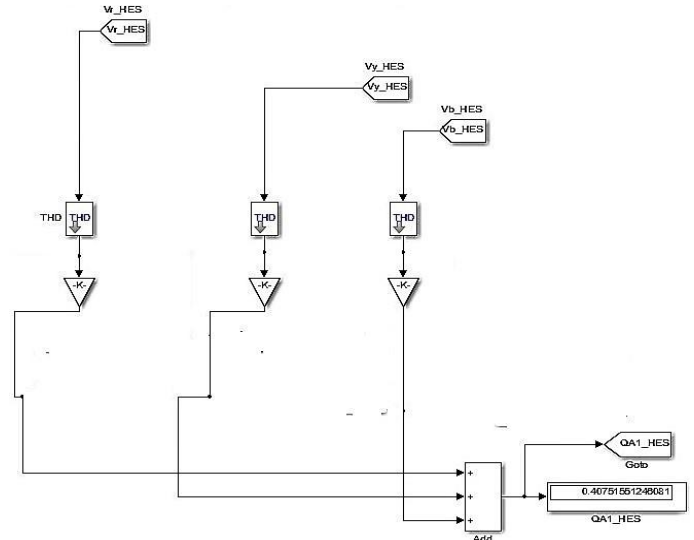


Fig. 16. QA_1 of the HES

The power quality analysis is verified in this paper for the HES and 3 ϕ load to find out the quality of power. The QA_1 , QA_2 , QA_3 , QA_4 and QA_5 of the HES as described in eqs. 26, 27, 32, 34 and 35 respectively, are simulated by the help of Matlab/Simulink. Fig.16 represents the model of QA_1 , where the value of QA_1 is found to be 0.4075155. In this manner QA_2 value of 0.3100727, QA_3 value of 0.7072647, QA_4 value of 0.7072647 and QA_5 of 2.74128507 of the HES are obtained. Hence, Fig.17 shows the PQF, whose value is found to be 95.1265972. Also, the PQF analysis of the 3 ϕ load is done and verified to be same as those of HES.

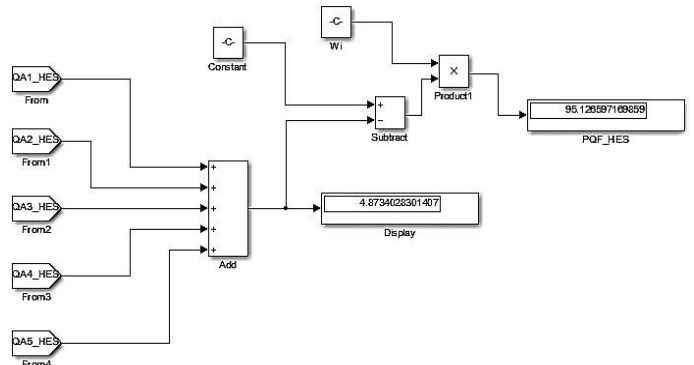


Fig. 17. PQF of the HES

The values of power quality analysis of the 3 ϕ non-linear load are found to be as $QA_1 = 0.4074447$, $QA_2 = 0.4644307$, $QA_3 = 0.7072625$, $QA_4 = 0.7540068$, $QA_5 = 2.74128507$ and $PQF = 94.92557$. Fig.18 shows the PQF the 3 ϕ non-linear load.

6. Conclusion

This paper presents a HES consisting of PV/FC/Electrolyzer with a storage tank. Different type of characteristics as well as system configuration of the various

HES sections are verified under simulation. Overall controls as well as power management strategy are also highlighted in this

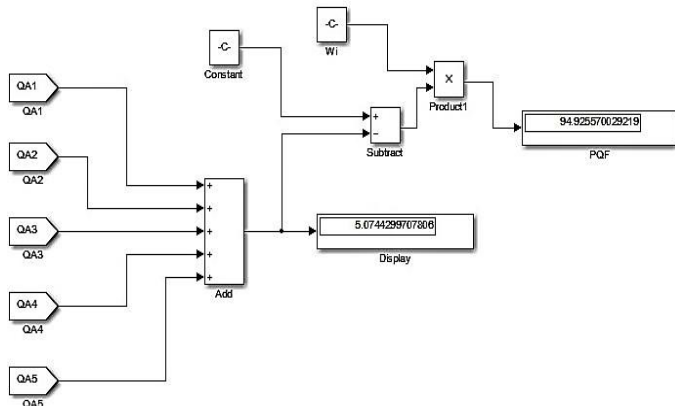


Fig. 18. PQF of the 3Ø non-linear load

paper. The proposed system is clean and environmental friendly system, where PV is used to generate the power, which is utilized for the 3Ø as well as 1Ø load and the extra energy source of PV if any is utilized for the production of H₂, which in the later stage is used as a fuel of SOFC. This SOFC is used when PV power is not sufficient for the load demand. Also this paper gives the information about the flow of H₂ to the SOFC through the valve that is controlled by the PID controller. Finally, PQF analysis is done for the HES and 3Ø non-linear load as the necessity of this PQF analysis is to measure the quality of power transfer.

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